# An analysis of the composite stellar population in M32\*

# P. Coelho<sup>1</sup>, C. Mendes de Oliveira<sup>2</sup>, R. Cid Fernandes<sup>3</sup> <sup>1</sup> Institut d'Astrophysique, CNRS, Université Pierre et Marie Curie, 98 bis Bd Arago, 75014 Paris, France (pcoelho@iap.fr)

- <sup>2</sup> Universidade de São Paulo, IAG, Rua do Matão 1226, São Paulo 05508-900, Brazil (oliveira@astro.iag.usp.br)
- 3 Departamento de Física, CFM, Universidade Federal de Santa Catarina, PO Box 476, 88040-900 Florianópolis, SC, Brazil (cid@astro.ufsc.br)

#### ABSTRACT

We obtained long-slit spectra of high signal-to-noise ratio of the galaxy M32 with the Gemini Multi-Object Spectrograph at the Gemini-North telescope. We analysed the integrated spectra by means of full spectral fitting in order to extract the mixture of stellar populations that best represents its composite nature. Three different galactic radii were analysed, from the nuclear region out to 2 arcmin from the centre. This allows us to compare, for the first time, the results of integrated light spectroscopy with those of resolved colour-magnitude diagrams from the literature. As our main result, we propose that an ancient and an intermediate-age population co-exist in M32, and that the balance between these two populations change between the nucleus and outside one effective radius  $(1 r_{\rm eff})$  in the sense that the contribution from the intermediate population is larger at the nuclear region. We retrieve a smaller signal of a young population at all radii whose origin is unclear and may be a contamination from horizontal branch stars, such as the ones identified by Brown et al. in the nuclear region. We compare our metallicity distribution function for a region 1 to 2 arcmin from the centre to the one obtained with photometric data by Grillmair et al. Both distributions are broad, but our spectroscopically derived distribution has a significant component with  $[Z/Z_{\odot}] \leq -1$ , which is not found by Grillmair et al.

Key words: stars: atmospheres, stars: evolution, galaxies: abundances, galaxies: evolution, galaxies: stellar content

# INTRODUCTION

M32 is a controversial galaxy. This low-mass satellite of M31 has long been considered the prototype of the *compact* elliptical morphological classification (Bender et al. 1992): low mass, high surface brightness galaxies, tidally truncated companions to massive galaxies. So far, few objects match this description (Ziegler & Bender 1998; Mieske et al. 2005; Chilingarian et al. 2007). The origins of the peculiar structural properties of M32 are still a matter of debate and the proposed models span a wide range of hypotheses: from a true elliptical galaxy at the lower extreme of the mass sequence to a threshed early-type spiral (Nieto & Prugniel

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1987; Bekki et al. 2001; Choi et al. 2002; Graham 2002; Gallagher et al. 2005; Young et al. 2008).

Controversial or not, M32 is a galaxy we need to understand because it plays an important role in resolving controversies about how to interpret the integrated spectra of galaxies: it is an early-type galaxy where we can get extremely high signal-to-noise (S/N) in the spectra, good coverage outside the nucleus to look for radial population gradients and resolve individual stars to a very meaningful magnitude level. If we hope to claim that we understand the evolution of distant early-type galaxies, we must first be able to demonstrate an understanding of M32 stellar population.

The stellar population of M32 has been extensively studied by means of integrated spectroscopy and resolved photometry. Most studies of the integrated spectrum of M32 have found signatures of an intermediateage and close to solar metallicity population (e.g. Rose 1985; Davidge 1990; Freedman 1992; Jones & Worthey 1995; Vazdekis & Arimoto 1999; del Burgo et al. 2001; Schiavon et al. 2004; Worthey 2004; Rose et al. 2005). The most commonly used technique of deriving mean-ages and mean-metallicities from integrated spectroscopy, as articulated by Worthey (1994), consists in comparing selected

Table 1. Parameter coverage of the fits. Adopted:  $Z_{\odot} = 0.017$ .

Model	$\log(\mathrm{age[yr]})$	$[{ m Z/Z}_{\odot}]$	Wavelength range (Å)
BC03 Charlot & Bruzual PEGASE-HR Vazdekis et al.	8.0 - 10.3 8.0 - 10.3 8.0 - 10.3 8.0 - 10.3	$\begin{array}{c} -2.2, -1.6, -0.6, -0.3, +0.05, +0.5\\ -2.2, -1.6, -0.6, -0.3, +0.05, +0.5\\ -1.6, -0.6, -0.3, +0.1, +0.05\\ -1.6, -1.2, -0.6, -0.3, +0.05, +0.25 \end{array}$	4700 - 8750 $4700 - 7400$ $4700 - 6800$ $4700 - 7400$

spectral indices to the predictions of simple stellar populations (SSP) models. Quoting an SSP-age and an SSP-metallicity, however, does not necessarily imply that a galaxy is an SSP. In fact, Bica et al. (1990) and Hardy et al. (1994) have shown that the spectral energy distribution of M32 cannot be adequately fit by SSP models, and Bica et al. (1990) argued that oversimplifications might explain some of the conflicting results found in literature (see also Oconnell 1980; Schmidt et al. 1989; Magris & Bruzual 1993; Rose 1994; Trager et al. 2000).

Resolved photometric studies include those Alonso-García et al. (2004) and Brown et al. who found signatures of a true ancient population in M32 by the identification of RR-Lyrae and an extended horizontal branch (HB), respectively, and Davidge & Jensen (2007) and references therein, who identified signatures of an intermediate age population. The most comprehensive study to date of the resolved stellar population of M32 has been carried out by Grillmair et al. (1996), who resolved individual stars down to slightly below the level of the HB with the Hubble Space Telescope (HST) Wide-Field Planetary Camera 2 (WFPC2) in a region 1-2 arcmin from the centre of the galaxy. The most striking feature of this colour-magnitude diagram (CMD; and also the one by Worthey et al. 2004, at a larger radii) is its composite nature, implying a range in [Z/H] from roughly solar down to below -1.0 dex.

Spreads in age and Z are as important as the mean values in understanding the star formation history of a galaxy, and a study that takes into account the composite stellar population of M32 may lead to a better understanding of its origin and evolution. In order to address this question, we obtained spectra of M32 along its major axis out to a radius of 2 arcmin, with the Gemini-North Telescope and Gemini Multi-Object Spectrograph (GMOS). We adopt the code STARLIGHT (Cid Fernandes et al. 2005) and state-of-the-art stellar population spectral models (Bruzual & Charlot 2003, hereafter BC03; Le Borgne et al. 2004, hereafter PEGASE-HR; Charlot & Bruzual in preparation, hereafter Charlot & Bruzual; Vazdekis et al. in preparation, hereafter Vazdekis et al.) to perform a pixel-by-pixel modelling of the integrated spectrum of M32. For the first time we extend the analysis of integrated spectra of M32 to the radii of the resolved CMD study by Grillmair et al. (1996).

Our observational data are described in Section 2, and we explain the analysis method in Section 3. Results are given in Section 4 and conclusions in Section 5.

## 2 OBSERVATIONAL DATA

Long-slit spectra of M32 were obtained on 2004 October 10, 11 and 16 with the GMOS on Gemini-North under the Program GN-2004B-Q-74. We used the R400 grating, a 0.75-arcsec slitwidth and an effective target wavelength at 6800 Å, resulting in spectra with coverage 4700 - 8930 Å and an average resolution of full width at half-maximum (FWHM)  $=5.4\,\text{Å}.$ 

Four exposures of 30s each were taken with the slit positioned over the nucleus of the galaxy, along the major axis of the galaxy [position angle (PA) =  $165^{\circ}$ ]. The slit was subsequently moved along the major axis off the central region to avoid contamination by scattered light (see Rose et al. 2005), and four long exposures of 3060s each were taken. The basic reduction tasks - trimming, bias and flat field correction - were done with the Gemini reduction package available for IRAF. The extraction of the spectra was then performed using the task APALL under the National Optical Astronomy Observatories (NOAO) long-slit reduction package. The spectra were extracted using the variance-weighted mode, with simultaneous extraction of the galaxy, sky and sigma spectra. The long GMOS slit (330 arcsec) allow us to measure the sky background in the same exposure as the galaxy spectrum, selected to be at the end of the slit.

From the short exposure observations, we extracted the nuclear spectra with an aperture of diameter of 1.5 arcsec. From the long off-centre exposures, two apertures were extracted in each exposure: one covering the radius from 30 to 60 arcsec (hereafter, position 1), and another covering from 1 to 2 arcmin (hereafter, position 2). In Fig. 1 it is shown a Digital Sky Survey image of M32 with the GMOS slit indicated, positioned for the long exposures. The apertures extracted as positions 1 and 2 are indicated as filled regions in the slit, as well as the region used to measure the sky background. The signal from position 1 is on average four times stronger than the background level (from eight times the sky level on the side closest to the nucleus, to three times in the darker side). The signal from position 2 is on average two times stronger than the background level (from three to 1.5 times). Position 2 was chosen to sample the same galactic radius observed by Grillmair et al. (1996) in its resolved photometric study, whose approximate field of view is indicated in Fig. 1 as a square.

The four spectra extracted at the central region have  $S/N^1$  S/N ranging from 34 to 43 pixel<sup>-1</sup> at 4750 Å, and from 180 to 230 pixel<sup>-1</sup> at 7000 Å. In the case of the long off-centre exposures, the spectra extracted for position 1 have

 $<sup>^1</sup>$  Computed as S/N=  $s_{\rm galaxy}/\sqrt{s_{\rm galaxy}+s_{\rm sky}},$  where  $s_{\rm galaxy}$  and  $s_{\rm sky}$  are the galaxy and sky spectra, respectively.

S/N ranging from 50 to 80 and from 270 to 470 pixel $^{-1}$ , at 4750 and 7000 Å respectively. The spectra for position 2 have S/N from 27 to 46 and from 152 to 267 pixel $^{-1}$  at the same wavelengths. The S/N of the two off-centre apertures drop rapidly beyond 7000 Å due to residuals of sky subtraction.

We have not flux calibrated the spectra as no spectrophotometric standard was observed in the nights of the observations. This will not hamper our analysis, as the full spectrum fitting technique adopted is not sensitive to the shape of the continuum.

#### 3 ANALYSIS

Full spectrum fitting techniques (e.g. Panter et al. 2003; Cid Fernandes et al. 2005; Mathis et al. 2006; Ocvirk et al. 2006a,b; Walcher et al. 2006; Koleva et al. 2008) have been used and validated in recent years as a powerful method for stellar population studies, and allows for fully exploiting the information present in our high-quality spectra of M32.

We employed a modified version of the STARLIGHT code by Cid Fernandes et al. (2005) in order to analyse the observed spectra. STARLIGHT combines spectra from a user-defined base of individual spectra in search for linear combinations that match an input observed spectrum. We adopt medium spectral-resolution simple SSP models spanning different ages and metallicities as our spectral base (described further in the text), i.e., we describe the data in terms of a superposition of multiple bursts of star formation.

To explore the parameter space defined by the linear coeficients associated with each population, the code uses a series of Markov Chains, each starting from different locations. The likelyhood surface is explored with a simulated annealing scheme, consisting of a succession of steps where  $\chi^2$  values are scaled by a gradually decreasing artificial 'temperature' (in analogy with Boltzmann factors in statistical mechanics), and parameter changes are performed with the Metropolis algorithm. In the computation of  $\chi^2$  each spectral pixel is weighted by its correspondent error, but bad pixels (the two CCD gaps in GMOS), strong telluric absorption features and residuals from sky subtraction are masked out. Pixels which deviate by more than three times the rms between the observed spectrum and the initial estimate for the model spectrum are also given zero weight. The internal kinematics is determined simultaneously with the population parameters. The fitted coefficients define a population vector (light fractions  $\mathbf{x}_i$  at a reference wavelength of 5000 Å), which gives the combination of SSP models in the base that best fits (smallest  $\chi^2$ ) the observed spectrum. This same combination of techiques has proved useful in several studies of the star formation history of galaxies of different types (see, e.g., Asari et al. 2007 and the STARLIGHT user manual $^2$  for examples).

For the present work, the public version of the code was modified to allow the use of continuum-normalized spectra (as opposed to flux-calibrated spectra). A simple moving average scheme of  $200\,\text{Å}$  windows (excluding masked points) was used to remove the continuum shape of both model

and observed spectra. This method fits all the pixels independently of the continuum, being therefore insensitive to extinction or flux calibration errors. The differences between flux-calibrated versus continuum-normalized spectral fitting have not been extensively studied vet. Wolf et al. (2007) compare four methods of deriving population parameters from integrated stellar cluster spectra, and their results favour the use of continuum-normalized spectra, as this method performed better in simultaneously retrieving age and metallicity for the clusters. We also performed a preliminary test using both versions of STARLIGHT on the public globular cluster spectra by Schiavon et al. (2005). We found that the two code versions yield results that agree typically within 0.2 dex in age, and 0.3 dex in metallicity. It is possible, therefore, that the same analysis applied on a set of flux-calibrated spectra would retrieve slightly different results than the ones presented here.

Spectral SSP models, adopted as base spectra, are undergoing constant revisions, following the improvement of their two main ingredients: stellar tracks and stellar spectral libraries. As our aim is to shed some light on the composite nature of M32 stellar population, without being biased by a particular choice of models, we opted for performing the analysis using four different sets of models: BC03, PEGASE-HR, Charlot & Bruzual and Vazdekis et al.<sup>3</sup>. The two latter are preliminary versions of new models being developed on the basis of the work by BC03 and Vazdekis (1999) respectively, using the MILES (Medium resolution INT Library of Empirical Spectra) empirical library (Sánchez-Blázquez et al. 2006a; Cenarro et al. 2007). BC03, Charlot & Bruzual and PEGASE-HR models were computed adopting evolutionary tracks by Bertelli et al. (1994), and Vazdekis adopted tracks by Girardi et al. (2000). BC03 and Charlot & Bruzual adopt initial mass function (IMF) from Chabrier (2003) and PEGASE-HR and Vazdekis et al. adopt the IMF from Salpeter (1955). For the fit procedure, we selected a range of ages between 100 Myr and 15 Gyr, spaced in log(age) = 0.25 dex. For the metallicites Z we adopted the full range provided by each set of models. The minimum wavelength of the fit is set by the observations (4700 Å), and the maximum is set by the base models (see Table 1).

The chosen models are all based on empirical stellar spectral libraries and as such are characterized by the abundance pattern typical of the Milky Way. Models such as those by Coelho et al. (2007) can in principle be used with spectral fitting techniques to extract information of the  $\alpha$ -enhancement in integrated light-studies. We do not consider such models in the present study, however, as we understand that an analysis of the  $\alpha$ -enhancement would add an extra free parameter to an already delicate analysis. This will not hamper our conclusions, as Worthey (2004) has shown that non-solar abundance ratio effects are mild in the case of M32, and do not change the population parameters significantly.

In total 48 STARLIGHT fits were performed (three galactic positions × four exposures for each position × four sets of base models). Examples of the fits performed by STARLIGHT are illustrated in Figures 2, 3 and 4 for the models BC03, Pegase-HR and Vazdekis et al. respectively. A measure of

<sup>&</sup>lt;sup>2</sup> http://www.starlight.ufsc.br/

<sup>&</sup>lt;sup>3</sup> http://www.iac.es/galeria/vazdekis/vazdekis\_models\_ssp\_seds.html

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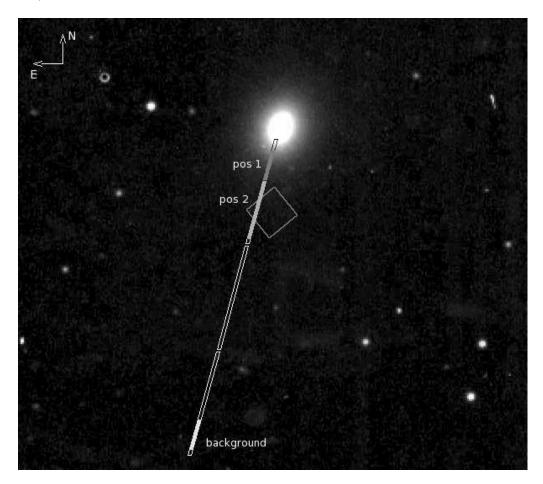


Figure 1. Digitized Sky Survey image of the field containing M32. The GMOS slit positioned for the long-exposures is illustrated, with Position 1, Position 2 and sky background apertures indicated as filled regions inside the slit. The GMOS slit is in total 330 arcsec long. The square indicates the approximate position of the HST field studied by Grillmair et al. (1996). The two discontinuities indicated in the slit correspond to the CCD gaps.

the quality of the fit is given by the average absolute deviation  $\overline{\Delta}$ :

$$\overline{\Delta} = \frac{1}{N} \sum_{\lambda} \left| \frac{(f_{\text{model}}(\lambda) - f_{\text{obs}}(\lambda))}{f_{\text{obs}(\lambda)}} \right| \tag{1}$$

where N is the number of pixels,  $f_{\rm model}$  is the fitted spectrum and  $f_{\rm obs}$  is the observed spectrum. Typically the model spectra reproduces the observed within 2 per cent of residual flux (see Table 2).

## 4 RESULTS

The analysis was performed with each observed spectrum individually, and the light-fraction vectors  $\mathbf{x}_j$  obtained by STARLIGHT were averaged over the four exposures for each combination of base models and radius. The results of  $\mathbf{x}_j$  are qualitatively shown in Fig. 5, as a function of  $\log(\text{age})$  and  $[\mathbf{Z}/\mathbf{Z}_{\odot}]$ , and in tabular form in the Appendix A. The projections of the averaged  $\mathbf{x}_j$  in the  $\log(\text{age})$  and Z planes give the age distribution functions (ADFs) and metallicity distribution functions (MDFs), shown in Figs 6 and 7, respectively.

It is worth remembering that the inversion from an ob-

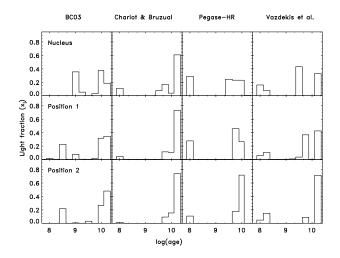


Figure 6. Age distribution functions obtained for each observed aperture (in rows) and each set of models (in columns), according to the labels.

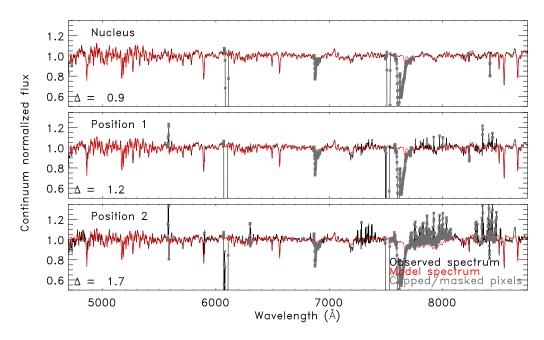


Figure 2. Observed spectra of M32 (black lines) and model spectra (red lines), for the three different observed apertures as indicated by the labels. Masked and rejected pixels are indicated as grey points. The average absolute deviation  $\overline{\Delta}$  of the fit (see text) is shown in each panel. Base models for these runs are BC03.

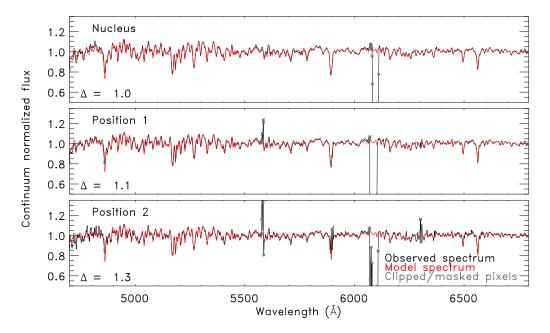


Figure 3. Same as in Figure 2, using PEGASE-HR as base models.

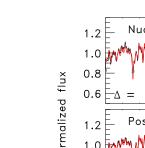
served spectrum to a set of parameters is a complex and degenerate problem, and we should avoid overdetailed descriptions of the population mixture (Ocvirk et al. 2006a). With that caveat in mind, we draw the following conclusions.

ancient population were obtained from photometric studies, both for the central region (Brown et al. 2000, 2008) and the outer reaches of the galaxy,  $\sim 3 \, \mathrm{arcmin}$  away from the centre (Alonso-García et al. 2004).

# 4.1 The distribution of ages

The age distribution has two to three peaks, depending on the base model. Signal of an ancient population [log(age)  $\geqslant 10$ ] is retrieved in all positions. Previous evidence of the

Intermediate-age populations [log(age) between 9.0 and 9.9] are also always retrieved. Most of the previous spectral studies find a mean intermediate age for the population of M32 (e.g. Rose et al. 2005 find a SSP age between 4 and 7 Gyr, depending on the radius), and the existence of such



Nucleus Continuum normalized flux 1.0 Position 1 0.8 0.6 Position 2 1.2 1.0 0.8 Model spectrum Clipped/masked pixels 5000 5500 6000 6500 7000 Wavelength (Å)

Figure 4. Same as in Figure 2, using Vazdekis et al. as base models.

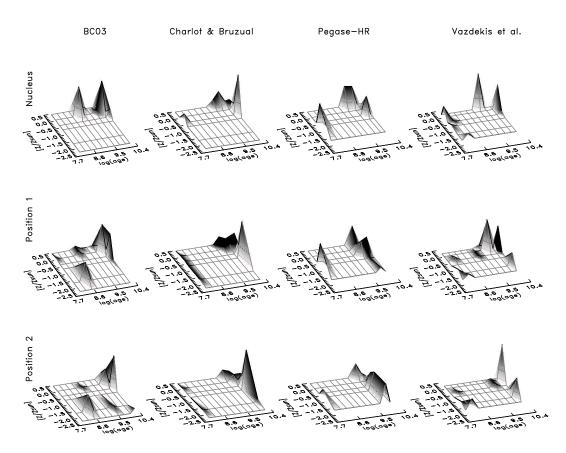


Figure 5. Representation of the light-fraction vectors  $x_j$  as a function of log(age) and  $[Z/Z_{\odot}]$ . The results for the nucleus, positions 1 and 2 are shown at the top, middle and bottom rows, respectively. Each column shows the results for a different set of base models, as indicated at the top of the figure. The light-fractions are given in tabular form in the appendix.

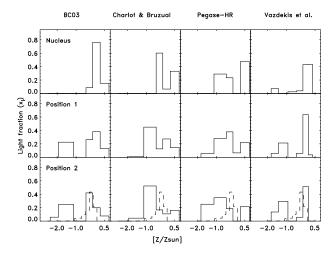


Figure 7. Metallicity distribution functions obtained for each observed aperture (in rows) and each set of models (in columns), according to the labels. The dashed line in the panels for Position 2 correspond to the empirical metallicity distribution function by Grillmair et al. (1996).

population also has been supported by the photometric studies by Davidge & Jensen (2007) and references therein.

In many cases, the inversion algorithm retrieves small amounts of a young population  $[\log(age) < 9.0]$ ), typically stronger in the runs with PEGASE-HR models. Rose et al. (2005) noted that a population in M32 cannot be any younger than 2 Gyr, or it would produce a strong signature in the Ca II index. As our spectrum does not extend blueward than 4800 Å, the Ca II region is not considered in the fit. The determination of ages in integrated spectra may be a difficult problem, as extended horizontal branch morphologies and/or blue stragglers, unaccounted for in the SSP models, can mimic young ages (de Freitas Pacheco & Barbuy 1995; Maraston & Thomas 2000; Trager et al. 2005). Interpretation of integrated globular cluster spectra from Schiavon et al. (2005) with STECMAP (STEllar Content via Maximum A Posteriori; Ocvirk et al. 2006a) supports the idea that blue HB stars in old metal-poor populations might appear as a spurious young burst of star formation (Koleva et al. 2007, 2008, Ocvirk, private communication). Hot HB stars in the central regions of M32 have been found by Brown et al. (2000), and thus it is possible that a least a fraction of the young population retrieved here is a signal of these hot old stars.

# 4.2 The distribution of abundances

The MDFs functions are smoother than the age distributions, with one or two peaks. In most of the cases, the peak of the metallicity distribution is centred at sub-solar values.

Position 2, the farthest from the nucleus, samples the same radius that was observed by Grillmair et al. (1996). The metallicity distribution obtained in that work is overplotted to our distributions as a dashed line in Fig. 7. Our results are in agreement with the conclusion by Grillmair et al. that the metallicity distribution in M32 is broad. On the

other hand, they obtain a distribution which is poor in stars with  $[Z/Z_{\odot}] \leq -1$ . This is, in contrast, an important fraction in our mixtures regardless of the base models adopted.

Several effects may be hampering the comparison between the photometric and the spectroscopic metallicity distributions. The MDF by Grillmair et al. (1996) is based on the colour distribution of red giant branch (RGB) stars, and as such it is affected by observational errors and age effects (their distribution assumes a constant age of 10 Gyr). Furthermore, the set of underlying isochrones of the spectral models used by the present work (Bertelli et al. 1994; Girardi et al. 2000) is different from the isochrones used for the star counts in Grillmair et al. (Worthey et al. 1994). Moreover, the MDF by Grillmair et al. is in the form of number of stars per Z bin, i.e., N(Z)dZ, while ours is a light-fraction MDF,  $L_{tot}(Z)dZ$ . In a general case where  $L_{tot}$ is not constant with Z, then N(Z) and L(Z) are not the same, and one should not expect a perfect match. As pointed out by the anonymous referee, one might not expect an MDF derived from spectroscopic data to match an MDF derived from photometric data unless biases and observational errors are properly taken into account.

In the mixtures retrieved by our analysis, the metal-poor component corresponds to a population younger than the metal-rich one (according to Fig. 5 and Tables A1—A9). It would be particularly puzzling if this trend is real, as it is in general expected that younger populations are formed from interstelar material already processed by older populations, and thus should be more metal-rich. On the other hand, in some cases this younger metal-poor population appears at the edges of the parameter space covered by the models, what might be an indication of an artefact effect.

# 4.3 Mean population parameters

The majority of the previous studies of M32 stellar populations publish the age and metallicities derived by the comparison to SSP models. Contrary to what is sometimes assumed, the SSP-equivalent ages and metallicities are not the same as the luminosity-weighted age and metallicites (see e.g. Trager et al. 2000; Walcher et al. 2006; Trager & Somerville 2009).

We computed the luminosity-weighted parameters of our population mixtures by adopting:

$$\langle \log(\text{age}) \rangle = \sum_{j} x_{j} \cdot \log(\text{age})_{j}$$
 (2)

and

$$\langle [Z/Z_{\odot}] \rangle = \sum_{j} x_{j} \cdot [Z/Z_{\odot}]_{j} \tag{3}$$

where the vector  $\mathbf{x}_j$  gives the normalized light-fraction of the jth SSP component of the model fit  $(\sum_j \mathbf{x}_j = 1)$ . The SSP-equivalent parameters, on the other hand, are the age and metallicity of the jth SSP which best fits the observed spectrum (smallest  $\overline{\Delta}$ ).

We list both the luminosity-weighted and SSP-equivalent parameters in Table 2, derived independently from each of the four exposures. It can be seen that the difference from adopting distinct base models is larger than the variance of the STARLIGHT runs on the four exposures of each position.

 $\textbf{Table 2.} \ \text{Light-weighted mean parameters and SSP-equivalent parameters obtained from the fits.} \ \text{Results are given for individual observed spectra.}$ 

		Light-weig	ghted para	meters	Best SSI	P fit paran	neters
Region	Obs #	Age[Gyr]	$[{\rm Z}/{\rm Z}_{\odot}]$	$\overline{\Delta}[\%]$	$\rm Age[Gyr]$	$[{\rm Z}/{\rm Z}_{\odot}]$	$\overline{\Delta}$ [%]
			BC03	}			
Nucleus	1	4.0	0.12	0.93	3.2	0.07	0.94
	2	4.5	0.09	0.98	3.2	0.07	0.98
	3	4.6	0.07	0.97	3.2	0.07	0.97
	4	4.1	0.12	1.00	3.2	0.07	1.00
Position 1	1	5.4	-0.13	1.14	10.0	-0.33	1.18
	2	3.7	-0.38	1.09	15.0	-0.33	1.14
	3	3.8	-0.45	1.14	15.0	-0.33	1.20
	4	3.6	-0.49	1.19	15.0	-0.33	1.24
Position 2	1	7.8	-0.55	2.11	10.0	-0.33	2.13
	2	4.6	-0.65	1.51	5.5	-0.33	1.52
	3	5.6	-0.66	1.54	10.0	-0.33	1.57
	4	4.6	-0.63	1.65	10.0	-0.33	1.65
			harlot & B		<u> </u>		
Nucleus	1	6.1	-0.05	0.89	5.5	0.07	0.95
	2	6.4	-0.03	0.94	5.5	0.07	0.99
	3	6.8	-0.02	0.93	5.5	0.07	0.96
	4	6.3	-0.04	0.96	5.5	0.07	1.00
Position 1	1	6.8	-0.21	1.02	10.0	-0.33	1.04
	2	10.0	-0.25	1.05	10.0	-0.33	1.09
	3	11.7	-0.26	1.01	10.0	-0.33	1.04
	4	13.3	-0.28	1.03	10.0	-0.33	1.05
Position 2	1	11.5	-0.49	1.93	10.0	-0.33	1.95
	2	10.8	-0.30	1.33	5.5	-0.33	1.35
	3	12.6	-0.33	1.37	10.0	-0.33	1.40
	4	12.8	-0.37	1.45	5.5	-0.33	1.49
			Pegase-	HR			
Nucleus	1	1.7	-0.03	1.04	3.0	0.07	1.04
	2	1.5	-0.04	1.10	3.0	0.07	1.11
	3	2.0	-0.03	1.07	3.0	0.07	1.07
	4	1.9	-0.03	1.10	3.0	0.07	1.10
Position 1	1	3.6	-0.37	1.13	6.0	-0.33	1.18
	2	1.7	-0.25	1.11	6.0	-0.33	1.13
	3	1.9	-0.25	1.10	6.0	-0.33	1.12
	4	2.0	-0.25	1.13	6.0	-0.33	1.15
Position 2	1	8.8	-0.78	2.06	3.0	-0.33	2.10
	2	4.2	-0.49	1.23	3.0	-0.33	1.27
	3	4.7	-0.52	1.28	3.0	-0.33	1.32
	4	5.6	-0.55	1.31	3.0	-0.33	1.35
			Vazdekis				
Nucleus	1	2.3	-0.02	0.97	3.2	0.05	0.97
	2	2.4	0.02	1.01	3.2	0.05	1.02
	3	2.7	-0.08	1.01	3.2	0.05	1.01
	4	2.5	-0.01	1.04	3.2	0.05	1.04
Position 1	1	3.9	-0.37	1.07	5.6	-0.33	1.11
	2	4.5	-0.30	1.13	3.2	0.05	1.17
	3	5.0	-0.30	1.15	3.2	0.05	1.18
	4	5.3	-0.38	1.23	5.6	-0.33	1.26
Position 2	1	4.3	-0.68	1.95	5.6	-0.33	1.99
	2	5.2	-0.53	1.39	3.2	-0.33	1.38
	3	6.5	-0.52	1.41	5.6	-0.33	1.44
	4	8.0	-0.58	1.52	10.0	-0.63	1.52

Table 3. Average luminosity-weighted parameters.

Region	Age (Gyr)	$[{\rm Z}/{\rm Z}_{\odot}]$
Nucleus Position 1 Position 2	$BC03$ $4.3 \pm 0.3$ $4.1 \pm 0.9$ $5.7 \pm 1.5$	$0.1 \pm 0.1$ $-0.4 \pm 0.2$ $-0.6 \pm 0.1$
Cl	narlot & Bruz	ual
Nucleus	$6.4 \pm 0.3$	$0.0 \pm 0.1$
Position 1	$10.4 \pm 2.8$	$-0.2 \pm 0.1$
Position 2	$11.9 \pm 0.9$	$-0.4 \pm 0.1$
	Pegase-HR	
Nucleus	$1.8 \pm 0.2$	$0.0 \pm 0.1$
Position 1	$2.3 \pm 0.9$	$-0.3 \pm 0.1$
Position 2	$5.8 \pm 2.1$	$-0.6 \pm 0.1$
	Vazdekis et al	
Nucleus	$2.5\pm0.2$	$0.0 \pm 0.1$
Position 1	$4.7 \pm 0.6$	$-0.3 \pm 0.1$
Position 2	$6.0 \pm 1.6$	$-0.6 \pm 0.1$

## 4.4 Evidence for gradients?

Studies of radial colour and line strength gradients have led to discordant results in recent years (see discussion in Rose et al. 2005, and references therein). In the present work, we opted for maximising the S/N (a critical issue in spectral fitting technique, see e.g. Koleva et al. 2007), and thus we have not split our spectra in many apertures to perform a detailed gradient study. In general terms, it is possible to identify in our analysis a shift in the distribution of populations, in the sense that the fraction coming from an old population is higher in the outer regions than in the nucleus. In order to statistically address this issue, in Table 3 we show the light-weighted parameters from Table 2 averaged on the four exposures, with their corresponding  $1\sigma$ uncertainties. A trend of higher ages and lower metallicities as one moves from the nucleus to position 2 can be seen in all cases, even though the gradient slopes are model-dependent.

These findings supports one of the scenarios discussed by Rose et al. (2005), in which there is a shifting balance between the populations with radii. A recent burst of starformation on top of an ancient population would appear as a higher concentration of a younger and more metal-rich population in the nucleus. This scenario would be a natural result of the model proposed by Bekki et al. (2001), in which centralised star formation in M32 is triggered by the tidal field of M31. On the other hand, HST near-ultraviolet (UV) imaging of M32 by Brown et al. (1998) reveals that the resolved UV-bright stars are more centrally concentrated than the underlying unresolved UV sources. Thus, it is also possible that the trend we see is a changing influence of a relatively small hot population prevalent in the nucleus. As the models do not vet consider hot stars in old populations. it is not possible with the present analysis to distinguish if it is the hot-old stars or the hot-young stars (or a combination of both) which is driving this balance shift.<sup>4</sup>

# 4.5 Dependence of the results with wavelength range

For the main fitting runs we opted for maximizing the use of information and thus to perform the fitting on the total wavelength range allowed by each set of spectral models. We additionally performed tests fitting only the region which is common to all base models (4700-6800 Å) and a limited region encompassing the most commonly used Lick/IDS (Lick Observatory Image Dissector Scanner) indices (4828-5363 Å), from H $\beta$  to Fe5335).

The results fitting only the region 4700-6800 Å are not strongly different from those obtained when fitting the whole range, except that lower weight is given to the old populations, and thus mean ages which are roughly 1 Gyr younger are derived. In the case of fitting the 4828-5363 Å region, the ages retrieved are slightly older in the nucleus but younger in the outer regions, and thus the gradient is flatter. The MDFs do not change significantly, except that the mean metallicity is slightly higher when only the 4828-5363 Å range is fitted.

The dependence of the results on wavelength range is an expected behavior for galaxies with star formation histories that are not well represented by a single burst (e.g. Sánchez-Blázquez et al. 2006b; Schiavon 2007). Therefore, we favor the use of wide wavelength ranges in analyses that aim at studying composite stellar populations.

#### 5 SUMMARY AND CONCLUSIONS

We obtained high S/N integrated spectra of the galaxy M32 with the GMOS at Gemini-North, out to 2 arcmin (3.6  $r_{\rm eff}$ ) from the centre of the galaxy. We performed an analysis of the composite stellar population in M32 using STARLIGHT by Cid Fernandes et al. (2005), a technique of full spectrum fitting, and adopting different sets of medium spectral resolution stellar population models: Bruzual & Charlot (2003), Le Borgne et al. (2004), Charlot & Bruzual (in prep.) and Vazdekis et al. (in prep.). Three different regions of the galaxy were analysed separately, the nuclear region, a region from 30 to 60 arcsec, and a region from 1 to 2 arcmin.

We can find mixtures of populations that reproduce our observed spectra within 2 per cent of residual flux. We find that in the nuclear region, 23–65 per cent (depending on the model used) of the light at 5000 Å comes from an ancient population [older than log(age) = 10], and intermediate-age populations [log(age) between 9 and 9.9] contribute to 25–48 per cent of the light. Beyond  $1\,r_{\rm eff}$  ( $r_{\rm eff}\sim33^{\circ}$ ), the light coming from the ancient population increases (27–90 per cent) and the contribution from intermediate-age populations decreases (4–41 per cent). There is a signal of a young-population [log(age) younger than 9.0] that contributes up to 30 per cent. As no evidence of such young

findings is the one proposed recently by Kormendy et al. (2009). In this formation scenario, the young light in the centre would be the result of a starburst in the latest dissipative merger that made the galaxy. There is a gradual change as radius increases, towards larger contributions from older stars that formed before the most recent merger(s). In this scenario, the gradient would be therefore intrinsic to the formation process of M32, and not triggered by M31.

<sup>&</sup>lt;sup>4</sup> Note added in proof: An alternative scenario to explain our

population has been found by previous photometric and spectroscopic studies, it is likely that at least part of this populations is a spectral signal of the hot HB stars identified by Brown et al. (2000). These findings suggest that the lack of spectral population models accounting for these hot old stars may set a constraint in our ability to identify the detailed age distribution of a galaxy from its integrated spectrum.

The metallicity distribution is peaked at subsolar values, and we retrieve a non-negligible contribution from a metal-poor population with  $[Z/Z_{\odot}] \leq -1.0$ . Such metal-poor population has not been identified in the CMD analysis such as Grillmair et al. (1996). As our position 2 samples the same radius as the analysis by Grillmair et al., this disagreement between integrated light studies and resolved stellar studies has yet to be understood.

As the main result of the present analysis, we propose that an ancient and an intermediate-age population co-exist in M32, in agreement with the photometric evidence found by e.g. Brown et al. (2000); Alonso-García et al. (2004) (for an old population) and Davidge & Jensen (2007) (for an intermediate age population). Moreover, we propose that the balance between these two populations change from the nucleus to the halo (outside  $1\,r_{\rm eff}$ ) in the sense that the contribution from the intermediate population is larger at the nuclear region.

More detailed descriptions of the age and metallicity distributions in M32 may have to wait for future stellar population models, as the balance of populations that fit our high-quality integrated spectra is model-dependent.

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# REFERENCES

- Alonso-García J., Mateo M., Worthey G., 2004, AJ, 127, 868
- Asari N. V., Cid Fernandes R., Stasińska G., Torres-Papaqui J. P., Mateus A., Sodré L., Schoenell W., Gomes J. M., 2007, MNRAS, 381, 263
- Bekki K., Couch W. J., Drinkwater M. J., Gregg M. D., 2001, ApJL, 557, L39
- Bender R., Burstein D., Faber S. M., 1992, ApJ, 399, 462 Bertelli G., Bressan A., Chiosi C., Fagotto F., Nasi E., 1994, AAPS, 106, 275
- Bica E., Alloin D., Schmidt A. A., 1990, Astronomy and Astrophysics, 228, 23
- Brown T. M., Bowers C. W., Kimble R. A., Sweigart A. V., Ferguson H. C., 2000, ApJ, 532, 308

- Brown T. M., Ferguson H. C., Stanford S. A., Deharveng J.-M., 1998, ApJ, 504, 113
- Brown T. M., Smith E., Ferguson H. C., Sweigart A. V., Kimble R. A., Bowers C. W., 2008, ApJ, 682, 319
- Bruzual G., Charlot S., 2003, MNRAS, 344, 1000
- Cenarro A. J., Peletier R. F., Sánchez-Blázquez P., Selam S. O., Toloba E., Cardiel N., Falcón-Barroso J., Gorgas J., Jiménez-Vicente J., Vazdekis A., 2007, MNRAS, 374, 664
- Chabrier G., 2003, ApJL, 586, L133
- Chilingarian I., Cayatte V., Chemin L., Durret F., Laganá T. F., Adami C., Slezak E., 2007, A&A, 466, L21
- Choi P. I., Guhathakurta P., Johnston K. V., 2002, AJ, 124, 310
- Cid Fernandes R., Mateus A., Sodré L., Stasińska G., Gomes J. M., 2005, MNRAS, 358, 363
- Coelho P., Bruzual G., Charlot S., Weiss A., Barbuy B., Ferguson J. W., 2007, MNRAS, 382, 498
- Davidge T. J., 1990, AJ, 99, 561
- Davidge T. J., Jensen J. B., 2007, AJ, 133, 576
- de Freitas Pacheco J. A., Barbuy B., 1995, A&A, 302, 718 del Burgo C., Peletier R. F., Vazdekis A., Arribas S., Mediavilla E., 2001, MNRAS, 321, 227
- Freedman W. L., 1992, AJ, 104, 1349
- Gallagher J. S., Grebel E. K., Smith L. J., 2005, in Jerjen H., Binggeli B., eds, IAU Colloq. 198: Near-fields cosmology with dwarf elliptical galaxies Making compact elliptical satellite galaxies: a conceptual model for M32. pp 151–155
- Girardi L., Bressan A., Bertelli G., Chiosi C., 2000, A&AS, 141, 371
- Graham A. W., 2002, ApJL, 568, L13
- Grillmair C. J., Lauer T. R., Worthey G., Faber S. M., Freedman W. L., Madore B. F., Ajhar E. A., Baum W. A., Holtzman J. A., Lynds C. R., O'Neil Jr. E. J., Stetson P. B., 1996, AJ, 112, 1975
- Hardy E., Couture J., Couture C., Joncas G., 1994, AJ, 107, 195
- Jones L. A., Worthey G., 1995, ApJL, 446, L31+
- Koleva M., Bavouzet N., Chilingarian I., Prugniel P., 2007,
  in Kissler-Patig M., Walsh J. R., Roth M. M., eds, Science
  Perspectives for 3D Spectroscopy Validation of Stellar
  Population and Kinematical Analysis of Galaxies. p. 153
- Koleva M., Prugniel P., Ocvirk P., Le Borgne D., 2007, in Vazdekis A., Peletier R. F., eds, IAU Symposium Vol. 241 of IAU Symposium, Age and metallicity of Galactic clusters from full spectrum fitting. pp 185–186
- Koleva M., Prugniel P., Ocvirk P., Le Borgne D., Soubiran C., 2008, MNRAS, 385, 1998
- Le Borgne D., Rocca-Volmerange B., Prugniel P., Lançon A., Fioc M., Soubiran C., 2004, A&A, 425, 881
- Magris G., Bruzual G., 1993, ApJ, 417, 102
- Maraston C., Thomas D., 2000, ApJ, 541, 126
- Mathis H., Charlot S., Brinchmann J., 2006, MNRAS, 365, 385
- Mieske S., Infante L., Hilker M., Hertling G., Blakeslee J. P., Benítez N., Ford H., Zekser K., 2005, A&A, 430, L25
- Nieto J.-L., Prugniel P., 1987, A&A, 186, 30
- Oconnell R. W., 1980, ApJ, 236, 430
- Ocvirk P., Pichon C., Lançon A., Thiébaut E., 2006a, MN-RAS, 365, 74

Ocvirk P., Pichon C., Lançon A., Thiébaut E., 2006b, MN-RAS, 365, 46

Panter B., Heavens A. F., Jimenez R., 2003, MNRAS, 343, 1145

Rose J. A., 1985, AJ, 90, 1927

Rose J. A., 1994, AJ, 107, 206

Rose J. A., Arimoto N., Caldwell N., Schiavon R. P., Vazdekis A., Yamada Y., 2005, AJ, 129, 712

Salpeter E. E., 1955, ApJ, 121, 161

Sánchez-Blázquez P., Gorgas J., Cardiel N., González J. J., 2006a, A&A, 457, 787

Sánchez-Blázquez P., Gorgas J., Cardiel N., González J. J., 2006b, A&A, 457, 809

Schiavon R. P., 2007, ApJS, 171, 146

Schiavon R. P., Caldwell N., Rose J. A., 2004, AJ, 127, 1513

Schiavon R. P., Rose J. A., Courteau S., MacArthur L. A., 2005, ApJS, 169, 163

Schmidt A., Bica E., Dottori H., Alloin D., 1989, Astrophysics and Space Science, 157, 79

Trager S. C., Faber S. M., Worthey G., González J. J., 2000, AJ, 120, 165

Trager S. C., Somerville R. S., 2009, ArXiv e-prints

Trager S. C., Worthey G., Faber S. M., Dressler A., 2005, MNRAS, 362, 2

Vazdekis A., 1999, ApJ, 513, 224

Vazdekis A., Arimoto N., 1999, ApJ, 525, 144

Walcher C. J., Böker T., Charlot S., Ho L. C., Rix H.-W., Rossa J., Shields J. C., van der Marel R. P., 2006, ApJ, 649, 692

Wolf M. J., Drory N., Gebhardt K., Hill G. J., 2007, ApJ, 655, 179

Worthey G., 1994, ApJS, 95, 107

Worthey G., 2004, AJ, 128, 2826

Worthey G., Faber S. M., Gonzalez J. J., Burstein D., 1994, ApJS, 94, 687

Worthey G., Mateo M., Alonso-García J., España A. L., 2004, PASP, 116, 295

Young C. K.-s., Currie M. J., Dickens R. J., Luo A.-L., Zhang T.-J., 2008, Chinese Journal of Astronomy and Astrophysics, 8, 369

Ziegler B. L., Bender R., 1998, A&A, 330, 819

### APPENDIX A: RESULTS

Population mixtures obtained for each set of SSP models, averaged on the four exposures (Tables A1-A12).

Table A1. Light percentage fraction as a function of age and Z for the nuclear region, obtained with BC03 models. The values for  $[\mathrm{Z}/\mathrm{Z}_{\bigodot}]$  are given in the column headers, log(age) is given in the first column. Adopted:  $\rm Z_{\bigodot} = 0.017.$ 

[Z/H] log(age)	-2.23	-1.63	-0.63	-0.33	0.07	0.47
8.00	0	0	0	0	0	0
8.25	0	0	0	0	0	0
8.50	0	0	0	0	0	0
8.75	0	0	0	0	0	0
9.00	0	0	0	0	36	0
9.25	0	0	0	0	0	5
9.50	0	0	0	0	0	0
9.75	0	0	0	0	3	0
10.00	0	0	0	0	38	0
10.18	0	0	0	9	0	10

Table A2. Same as in A1, but for position 1 and BC03 models.

[Z/H] log(age)	-2.23	-1.63	-0.63	-0.33	0.07	0.47
8.00	0	0	0	0	2	0
8.25	0	0	0	0	0	0
8.50	0	23	0	0	0	0
8.75	0	0	0	0	0	0
9.00	0	0	0	0	4	4
9.25	0	0	0	0	0	0
9.50	0	0	0	0	0	0
9.75	0	0	0	0	0	1
10.00	0	0	0	0	32	0
10.18	0	0	0	26	1	7

Table A3. Same as in A1, but for position 2 and BC03 models.

${\rm [Z/H]} \\ {\rm log(age)}$	-2.23	-1.63	-0.63	-0.33	0.07	0.47
8.00	0	0	0	0	0	0
8.25	0	0	0	0	0	0
8.50	0	21	0	0	0	0
8.75	0	0	0	0	0	0
9.00	0	0	0	0	1	0
9.25	0	0	0	0	0	0
9.50	0	3	0	0	0	0
9.75	0	0	0	0	0	0
10.00	0	0	0	0	19	8
10.18	6	0	0	42	0	0

Table A4. Same as in A1, but for the nuclear region and Charlot & Bruzual models.

[Z/H] $log(age)$	-2.23	-1.63	-0.63	-0.33	0.07	0.47
8.00	0	0	0	11	0	0
8.25	0	0	0	0	0	0
8.50	0	0	0	0	0	0
8.75	0	0	0	0	0	0
9.00	0	0	0	0	0	0
9.25	0	0	0	0	0	0
9.50	0	0	0	0	0	8
9.75	0	0	0	0	0	17
10.00	0	0	0	0	0	4
10.18	0	0	0	49	7	5

Table A5. Same as in A1, but for position 1 and Charlot & Bruzual models.

[Z/H] $log(age)$	-2.23	-1.63	-0.63	-0.33	0.07	0.47
8.00	0	1	1	2	1	0
8.25	0	0	0	0	0	0
8.50	0	0	0	0	0	0
8.75	0	0	0	0	0	0
9.00	0	0	0	0	0	0
9.25	0	0	0	0	0	0
9.50	0	0	0	0	0	0
9.75	0	0	0	0	2	9
10.00	0	0	0	0	5	5
10.18	0	0	44	11	18	0

Table A6. Same as in A1, but for position 2 and Charlot & Bruzual models.

[Z/H] log(age)	-2.23	-1.63	-0.63	-0.33	0.07	0.47
8.00	0	1	0	0	1	0
8.25	0	0	0	0	0	0
8.50	0	0	0	0	0	0
8.75	0	0	0	0	0	0
9.00	0	0	0	0	0	0
9.25	0	0	0	0	0	0
9.50	0	0	0	0	0	0
9.75	0	0	0	0	0	9
10.00	0	0	0	0	9	7
10.18	0	4	52	17	1	0

Table A7. Same as in A1, but for the nuclear region and PEGASE-HR models.

[Z/H] log(age)	-1.63	-0.63	-0.33	0.07	0.47
8.00	0	29	0	0	0
8.25	0	0	0	0	0
8.50	0	0	0	0	0
8.75	0	0	0	0	0
9.00	0	0	0	0	0
9.25	0	0	0	0	0
9.50	0	0	0	0	25
9.75	0	0	0	0	23
10.00	0	0	23	0	0
10.18	0	0	0	0	0

Table A8. Same as in A1, but for position 1 and PEGASE-HR models.

${\rm [Z/H]} \\ {\rm log(age)}$	-1.63	-0.63	-0.33	0.07	0.47
8.00	0	28	3	0	0
8.25	0	0	0	0	0
8.50	0	0	0	0	0
8.75	0	0	0	0	0
9.00	0	0	0	0	0
9.25	0	0	0	0	0
9.50	0	0	0	0	0
9.75	0	0	17	6	22
10.00	6	0	21	0	0
10.18	0	0	0	0	0

 ${\bf Table~A9.}$  Same as in A1, but for position 2 and PEGASE-HR models.

${\rm [Z/H]} \\ {\rm log(age)}$	-1.63	-0.63	-0.33	0.07	0.47
8.00	0	11	0	0	0
8.25	0	0	0	0	0
8.50	0	0	0	0	0
8.75	0	0	0	0	0
9.00	0	0	0	0	0
9.25	0	0	0	0	0
9.50	0	0	0	0	0
9.75	0	0	0	0	17
10.00	25	24	19	0	4
10.18	0	0	0	0	0

**Table A10.** Same as in A1, but for the nuclear region and Vazdekis et al. models.

[Z/H] log(age)	-1.63	-1.23	-0.63	-0.33	0.05	0.25
8.00	0	0	3	0	13	0
8.25	7	0	0	0	0	0
8.50	0	0	0	0	0	0
8.75	0	0	0	0	0	0
9.00	0	0	0	0	0	0
9.25	0	0	0	0	0	0
9.50	0	0	0	0	0	43
9.75	0	0	0	0	0	0
10.00	0	0	0	0	0	0
10.18	0	0	0	4	29	0

**Table A11.** Same as in A1, but for position 1 and Vazdekis et al. models.

[Z/H] log(age)	-1.63	-1.23	-0.63	-0.33	0.05	0.25
8.00	0	6	0	0	0	0
8.25	6	0	0	5	0	0
8.50	0	0	0	0	0	0
8.75	0	0	0	0	0	0
9.00	0	0	0	0	0	0
9.25	0	0	0	1	0	0
9.50	0	0	0	0	0	4
9.75	0	0	0	0	36	0
10.00	0	0	0	0	0	0
10.18	0	15	0	0	27	0

Table A12. Same as in A1, but for position 2 and Vazdekis et al. models.

[Z/H] log(age)	-1.63	-1.23	-0.63	-0.33	0.05	0.25
8.00	0	5	0	0	0	0
8.25	14	0	0	1	0	0
8.50	0	0	0	0	0	0
8.75	0	0	0	0	0	0
9.00	0	0	0	0	0	0
9.25	0	0	0	0	0	0
9.50	0	0	0	0	0	0
9.75	0	0	0	4	5	0
10.00	0	0	0	0	0	0
10.18	0	25	0	0	47	0